

Kinetics Worksheet #3
Integrated Rate Laws and Half-Life Problems

Ref: Dick Powell, Chemistry Teacher, Arlington, Texas, Personal Communication, July, 2003.

1. The reaction below shows first-order kinetics, and at 32°C the rate constant is $2.8 \times 10^{-2} \text{ min}^{-1}$. What is the half-life in minutes?



Answer = 24.75 min

$$t_{1/2} = \frac{.693}{2.8 \times 10^{-2}} = \boxed{24.75 \text{ min}}$$

2. $\text{A} \rightarrow \text{B} + \text{C}$: This reaction is second-order in A. If the initial concentration of A is 0.100 M, the reaction is 20% complete in 40.0 minutes. What is the rate constant value (and units)?

Answer = $0.0625 \text{ M}^{-1}\text{min}^{-1}$

$$[A]_0 = .100 \text{ M}$$

$$[A]_t = .080 \text{ M}$$

$$t = 40.0 \text{ min}$$

$$\frac{1}{.080} = k(40.0) + \frac{1}{.100}$$

$$2.5 = 40k$$

$$\boxed{k = .0625}$$

3. A particular first-order reaction has a rate constant of 0.33 min^{-1} . How many minutes will it take for a reactant concentration of 0.13 M to decrease to 0.088 M?

Answer = 1.2 min

1st order

$$k = .33$$

$$[A]_0 = .13 \text{ M}$$

$$[A]_t = .088 \text{ M}$$

$$\ln[.088] - \ln[.13] = (-.33)t$$

$$\boxed{t = 1.2 \text{ min}}$$

4. The rate law for the hydrolysis of sucrose is $\text{Rate} = k[\text{C}_{12}\text{H}_{22}\text{O}_{11}]$. After 2.57 hours at 25°C , 0.55 M of $\text{C}_{12}\text{H}_{22}\text{O}_{11}$ has decreased to 0.45 M. Calculate the rate constant value and units for this reaction.

1st order based on rate law in problem

Answer = 0.078 hr^{-1}

$$t = 2.57 \text{ hours}$$

$$[A]_0 = .55 \text{ M}$$

$$[A]_t = .45 \text{ M}$$

$$\ln [0.45] - \ln [0.55] = -k(2.57)$$

$$k = .078$$

5. The rate constant for the second-order decomposition of nitrogen dioxide, $\text{NO}_2 \rightarrow \text{NO} + \frac{1}{2} \text{O}_2$, is $3.40 \text{ M}^{-1} \text{ min}^{-1}$. Calculate the time, in minutes, needed to decrease the concentration of NO_2 from 2.00 M to 1.50 M.

Answer = 0.05 minutes

2nd order reaction

$$k = 3.40$$

$$[A]_0 = 2.00 \text{ M}$$

$$[A]_t = 1.50 \text{ M}$$

$$\frac{1}{1.50} = (3.40)(t) + \frac{1}{2.00}$$

$$.167 = 3.40t$$

$$t = .049 \text{ min}$$